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Turbulence Model Comparison for Compact Plate Heat Exchanger Design Application

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Abstract

In the framework of the Gas-Power Conversion System for the Advanced Sodium Technological Reactor for Industrial Demonstration (ASTRID) project design, works done at CEA are focused on the design of the sodium-gas heat exchanger. Compact plate heat exchangers are indicated as the most suitable technology for such applications.

An innovative compact heat exchanger geometry is proposed in this paper: its innovation consists in creating a 3D mixing flow. The proposed geometry has also very good mechanical resistance to high pressure gradients, being suitable for a large variety of flow applications.

The flowfield inside such a channel is experimentally studied using the Laser Doppler Velocimetry (LDV) technique. The main velocity, the radial velocity as well as the Reynolds stresses are measured: data show the high level of flow mixing and the 3D flow pattern inside the channel.

The experimental measurements are then used to validate turbulence models: in particular Reynolds-Averaged Navier-Stokes (RANS) equations are closed using both isotropic 2-equation isotropic eddy viscosity models and a Non-Linear Eddy Viscosity Model (NLEVM).

Presented results represent the first step in the assessment of innovative high-performance compact plate heat exchangers that can be used to increase the plant efficiency as well as decrease the capital cost of the single component.

I. INTRODUCTION

The ASTRID project is a French project aiming to build a GEN IV sodium fast reactor to burn minor actinides, to extend the availability of natural uranium resources still maintaining a safety and security level at least equal to that of current generation nuclear reactors¹. The sodium-water chemical interaction being one of the major issues for a safe operation of a SFR, a gas Brayton cycle has been investigated² to *de facto* eliminate the occurrence of such an accident. In particular, the best suited gas was found to be the nitrogen, having the best trade-off between plant efficiency and technological use. A number of studies has been done³ to evaluate the R&D program necessary to develop the sodium-gas heat exchanger, which is the critical component substituting the steam generator.

Conceptual designs of compact sodium-gas heat exchanger (SGHE) have been proposed⁴ (Figure 1) based on existing technologies such as the PCHE and the PSHE. Nitrogen has been chosen as the reference gas for such an application⁵.

The principle of the Sodium-Gas heat exchanger is to dispose modules of plates in a pressurized vessel which is also the header of the modules. The inlet/outlet of the nitrogen is located on the top of the component and the inlet/outlet of the sodium is on the bottom. More details can be found in reference⁶. The main issue of this development is to have the highest thermal compactness, and so the judicious choice of the gas flow pattern.

The literature showed how the more 3-D the flow is, the higher is the heat transfer coefficient. Hence, in order to increase the heat transfer coefficient (and the global compactness) the objective is to develop an innovative channel: specifically the channel is composed by elementary geometrical elements like bends, straight channels and mixing zones. Note that there is no available heat exchanger composed by such geometrical elements.

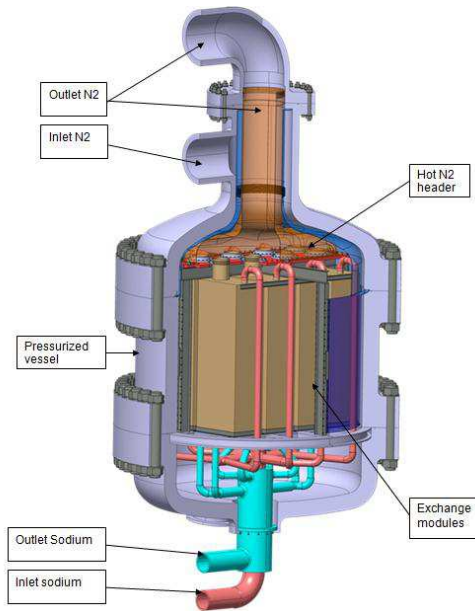


Figure 1 – Conceptual Design of the SGHE

A preliminary investigation made at CEA (based on RANS CFD computations) showed that the proposed double channel compact heat exchanger provides a higher compactness (expressed as the thermal power per unit volume of the component) than a commercial PCHE for the same thermal power and pressure drop, as Figure 2 shows.

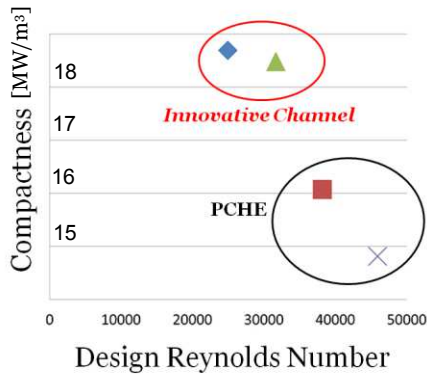


Figure 2 – Heat Transfer geometry compactness comparison

Hence, the need for a large database of fluid flow inside such a channel is of primary importance to validate the numerical model as well as the performance comparison with other heat transfer geometries.

The innovative channel is therefore the object of the present study. First of all some experimental measurements are shown that are a small part of the database collected. Then, based on the experimental data, a turbulence model validation is performed in order to

determine the most appropriate turbulence model to reproduce the characteristics of the actual flow. Note that the goal of the present paper is not to describe and explain in detail the physics of the flow but rather to validate a model against acquired experimental data. Moreover, as a first step, the current work does not take into account heat transfer inside the innovative geometry, being a pure aerodynamic validation.

II. EXPERIMENTAL MEASUREMENTS

II.A. Experimental setup

In order to show the primary and secondary fluid motion as well as the boundary layer behavior both for the in-bend and the mixing-zone flow, a LDV has been evaluated as the best measurement technique. In particular, due to its capability to measure boundary layers, a 2-C LDV setup has been used to measure the principal and the radial velocity. The experimental setup has been assembled at the ONERA-Toulouse center. The measurement chain is shown in Figure 3:

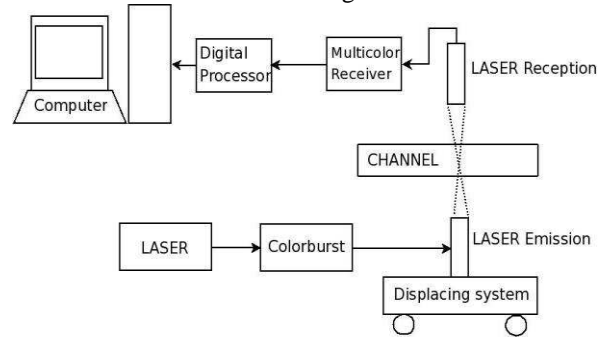


Figure 3 – LDV Experimental setup

The used technical means are a Spectra Physics Stabilité 2017 Laser, a TSI Colorburst Multicolor Beam Separator Model 9201 (both of them shown in Figure 4) to split blue and green beams used for the 2-C velocimetry and to provide the Bragg frequency shifting), an ISEL displacing system, a TSI Colorlink Plus Multicolor Receiver Model 9230 (to measure the laser reception frequency shifting) and a TSI FSA4000 Multibit Digital Processor (to provide digital data to the post-processing computer). The visualization particles are Di-Ethyl-Hexyl-Sebacat (DEHS) droplets.



Figure 4 – Laser and Beam Separator

Details on the laser beams are shown in Table I, whereas a view of the measurement volume is shown in Figure 5:

TABLE I
Laser Beams Data

Data/Color	Green	Blue
Wavelength [nm]	514.5	488.0
Beam Diameter [μm]	90.42	85.76
Beam intersection major dimension [mm]	1.32	1.25
Fringe Spacing [μm]	3.70	3.52
Bragg Frequency [MHz]	10	10

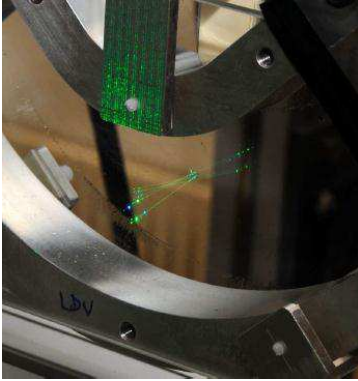


Figure 5 – Measurement Volume

The test section is composed by structural aluminum parts with glass windows where the LDV measurement is performed (see Figure 5).

The working fluid is air at atmospheric temperature and pressure. The inlet velocity is 13 m/s, to have a correspondent inlet Reynolds number of 50 600.

II.B. Measurements description

The full measurement campaign has been done on several channel cross sections in the bends as well as in the mixing zone. For the sake of space we will only discuss about a few of them, specifically two profiles in a bend and one profile in the mixing zone. The in-bend profiles lie in a plane having a 45° angular rotation from the bend inlet section. Refer to dotted lines in Figure 6 for their definition of line #1 and line #2:

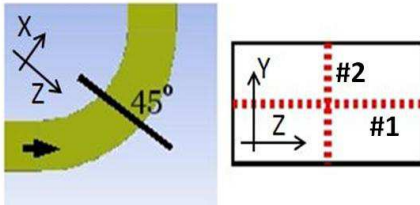


Figure 6 – In-Bend profiles definition

The mixing zone profiles are defined by dot #3 in Figure 7. Note that the profile is actually along the Y axis normal to the paper XZ plane.

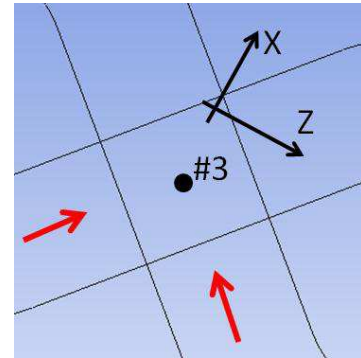


Figure 7 – Mixing zone profiles definition

II.C. Uncertainty evaluation

Three types of uncertainties have been identified during the experimental campaign, specifically the uncertainty due to the data acquisition chain, the uncertainty due to environmental conditions and the uncertainty due to the measurement volume position. Regarding the data acquisition chain uncertainty, the global system calibration gave a velocity standard deviation value never greater than 0.25% of the measured velocity. In order to evaluate the experimental uncertainties in our measurements, two specific tests have been made: first, to be able to quantify the influence of external parameters such as low frequency velocity fluctuations, optical quality of the test section all over the measurements, in-day temperature variations etc. we performed a repeatability test consisting in repeating several times (i.e. around 400 times for the in bend flow and around 200 times for the mixing zone flow) the measurement at the same position. Once collected this data, the uncertainty in the velocity has been calculated as the standard deviation of the sample with regard to the test mean value. Finally, to evaluate the uncertainty due to the measurement volume position, measurements have been done in the vertices of a cube centered in the reference point having the vertices at ± 0.2 mm from the center along the three axes X, Y, Z.

The final velocity uncertainty is calculated adding the three obtained variance, calculated as the 3σ where σ is the combined standard deviation determined by adding the variances of each source of uncertainty.

The final uncertainty analysis is shown in Table II and Table III. Note that the evaluation is strictly valid only for the points where the repeatability and the position uncertainty tests have been performed; nevertheless it gives a good idea of the global uncertainties for the actual flow.

TABLE II
Velocity U Uncertainty Analysis

	σ System Chain	σ Repeatability	σ Position	Total 3σ Uncertainty
In-bend	0.03 m/s	0.03 m/s	0.01 m/s	0.13 m/s
In-mixing zone	0.01 m/s	0.05 m/s	0.07 m/s	0.26 m/s

TABLE III
Velocity W Uncertainty Analysis

	σ System Chain	σ Repeatability	σ Position	Total 3σ Uncertainty
In-bend	0.001 m/s	0.05 m/s	0.14 m/s	0.45 m/s
In-mixing zone	0.01 m/s	0.05 m/s	0.07 m/s	0.26 m/s

TABLE IV
 uw Reynolds Stress Uncertainty Analysis

	σ System Chain	σ Repeatability	σ Position	Total 3σ Uncertainty
In-bend	0.06 m ² /s ²	0.04 m ² /s ²	0.05 m ² /s ²	0.26 m ² /s ²
In-mixing zone	0.04 m ² /s ²	0.19 m ² /s ²	0.14 m ² /s ²	0.72 m ² /s ²

Note that the position uncertainties are quite high and are responsible for a large part of the total uncertainty: indeed these high values are due to the high velocity gradients (hence the large amount of turbulence) in the fluid flow.

III. NUMERICAL VALIDATION

III.A. Turbulence model description

Three turbulence models have been used to test their ability to correctly represent the fluid flow inside the channel. In particular two isotropic eddy viscosity models (e.g. Realizable k - ϵ and k - ω SST), and a NLEVM will be compared. FLUENT[®] code has been used to perform calculations. Since the eventual goal of the study is to use a cost-effective numerical model for the design the

innovative heat exchanger, only two-equation RANS model are evaluated. Hence more complex models such as the Reynolds Stress Transport (RSM) models are out of the scope of this work.

The Realizable k - ϵ model was proposed firstly by Shih et al.⁷. The transport equations of the turbulent variables for an incompressible flow are:

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_j}(\rho k u_j) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + G_k - \rho \epsilon \quad (1)$$

$$\frac{\partial}{\partial t}(\rho \epsilon) + \frac{\partial}{\partial x_j}(\rho \epsilon u_j) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_\epsilon} \right) \frac{\partial \epsilon}{\partial x_j} \right] + \rho C_1 S \epsilon - \rho C_2 \frac{\epsilon^2}{k + \sqrt{\nu \epsilon}} \quad (2)$$

$$\mu_t = \rho C_\mu \frac{k^2}{\epsilon} \quad (3)$$

Where G_k is the turbulence kinetic energy production term. To be consistent with the Boussinesq hypothesis:

$$G_k = -\rho \overline{u_i' u_j'} \frac{\partial u_j}{\partial x_i} = \mu_t S^2 \quad (4)$$

with S being the modulus of the mean rate of strain tensor, defined as follows:

$$S = \sqrt{\frac{1}{2} S_{ij} S_{ij}} \quad (5)$$

The model is closed by the eddy viscosity formulation, where C_μ is defined as :

$$C_\mu = \frac{1}{A_0 + A_s \frac{k}{\epsilon} U^*} \quad (6)$$

$$\text{Where } U^* = \sqrt{S_{ij} S_{ij} + \overline{\Omega_{ij} \Omega_{ij}}} \quad (7),$$

$$A_0 = 4.04, A_s = \sqrt{6} \cos \phi, \phi = \frac{1}{3} \cos^{-1}(\sqrt{6} W),$$

$$W = \frac{S_{ij} S_{jk} S_{ki}}{S^3} \text{ and } \tilde{S} = \sqrt{\frac{1}{4} S_{ij} S_{ij}}$$

The coefficient C_1 is expressed as:

$$C_1 = \max \left[0.43, \frac{\eta}{\eta + 5} \right], \quad (8) \quad \eta = S \frac{k}{\epsilon} \quad (9)$$

The model constants are:

$$C_2 = 1.9, \sigma_k = 1.0 \text{ and } \sigma_\epsilon = 1.2.$$

To allow for integration up to the wall a Two-Layer Formulation is used: in particular, given the turbulent

Reynolds number $Re_y = \frac{\rho y \sqrt{k}}{\mu}$, for a $Re_y > 200$ the complete k- ϵ model is employed, i.e. both the transport equation for k and for ϵ are solved. For $Re_y \leq 200$ only the k-transport equation is solved, whereas the turbulence dissipation rate is calculated by a mixing length ℓ_ϵ evaluation as follows:

$$\epsilon = \frac{k^{3/2}}{\ell_\epsilon}, \ell_\epsilon = y C_\ell^* (1 - e^{-Re_y/A_\epsilon}) \quad (10)$$

The eddy viscosity is damped from the fully turbulent to the buffer region value by the following expression:

$$\mu_{t,2L} = \lambda_\epsilon \mu_t + (1 - \lambda_\epsilon) \mu_{t,buffer}, \quad (11)$$

$$\mu_{t,buffer} = \rho C_\mu \ell_\mu \sqrt{k}, \quad (12) \quad \ell_\mu = y C_\ell^* (1 - e^{-Re_y/A_\mu}), \quad (13)$$

$$\lambda_\epsilon = \frac{1}{2} \left[1 + \tanh \left(\frac{Re_y - 200}{A} \right) \right] \quad (14)$$

The model constants are:

$$C_\ell^* = \kappa C_\mu^{-3/4}, \quad \kappa = 0.4187, \quad A_\epsilon = 2C_\ell^*, \quad A_\mu = 68, \\ A = 17.41$$

The Shear Stress Transport (SST) model has been proposed by Menter⁸. Transport equations of the turbulent variables for an incompressible flow are:

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_j}(\rho k u_j) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + \widetilde{G}_k - \rho \beta^* k \omega \quad (15)$$

$$\frac{\partial}{\partial t}(\rho \omega) + \frac{\partial}{\partial x_j}(\rho \omega u_j) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_\omega} \right) \frac{\partial \omega}{\partial x_j} \right] + G_\omega - \rho \beta \omega^2 + D_\omega \quad (16)$$

The turbulent Prandtl numbers for k and ω are expressed in the following way:

$$\sigma_k = \frac{1}{\frac{F_1}{\sigma_{k,1}} + \frac{(1-F_1)}{\sigma_{k,2}}} \quad (17)$$

$$\sigma_\omega = \frac{1}{\frac{F_1}{\sigma_{\omega,1}} + \frac{(1-F_1)}{\sigma_{\omega,2}}} \quad (18)$$

The function F_1 is computed as:

$$F_1 = \tanh(\phi_1^4), \quad (19)$$

$$\phi_1 = \min \left[\max \left(\frac{\sqrt{k}}{0.09 \omega y}, \frac{500 \mu}{\rho y^2 \omega} \right), \frac{4 \rho k}{\sigma_{\omega,2} D_\omega^+ y^2} \right] \quad (20)$$

$$D_\omega^+ = \max \left[2 \rho \frac{1}{\sigma_{\omega,2}} \frac{1}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j}, 10^{-10} \right] \quad (21)$$

The turbulence kinetic energy production term in the SST models has a limiter, defined as:

$$\widetilde{G}_k = \min(G_k, 10 \rho \beta^* k \omega) \quad (22)$$

Where G_k is given by Eq.4.

The specific dissipation rate production is given by:

$$G_\omega = \frac{\rho \alpha}{\mu_t} \widetilde{G}_k, \quad (23) \quad \alpha = F_1 \alpha_{\infty,1} + (1 - F_1) \alpha_{\infty,2}, \quad (24)$$

$$\alpha_{\infty,1} = \frac{\beta_{i,1}}{\beta^*} - \frac{\kappa^2}{\sigma_{\omega,1} \sqrt{\beta^*}}, \quad (25)$$

$$\alpha_{\infty,2} = \frac{\beta_{i,2}}{\beta^*} - \frac{\kappa^2}{\sigma_{\omega,2} \sqrt{\beta^*}} \quad (26)$$

The coefficient β is expressed by :

$$\beta = F_1 \beta_{i,1} + (1 - F_1) \beta_{i,2} \quad (27)$$

The Cross-Diffusion term D_ω is expressed as follows:

$$D_\omega = 2(1 - F_1) \rho \frac{1}{\sigma_{\omega,2}} \frac{1}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j} \quad (28)$$

Finally the model is closed by the definition of the eddy viscosity:

$$\mu_t = \frac{\rho k}{\omega} \frac{1}{\max \left[1, \frac{S F_2}{a_1 \omega} \right]} \quad (29)$$

$$F_2 = \tanh(\phi_2^2), \quad (30) \quad \phi_2 = \max \left(\frac{2\sqrt{k}}{0.09 \omega y}, \frac{500 \mu}{\rho y^2 \omega} \right) \quad (31)$$

Model constants are:

$$\sigma_{k,1} = 1.176, \quad \sigma_{k,2} = 1.0, \quad \sigma_{\omega,1} = 2.0, \quad \sigma_{\omega,2} = 1.168, \quad \beta^* = 0.09, \quad a_1 = 0.31, \quad \beta_{i,1} = 0.075, \quad \beta_{i,2} = 0.0828.$$

With regard to the NLEVM, the adopted model is that of Baglietto et al.⁹(which has been implemented in FLUENT® via specific User Defined Functions). In particular this is a modified version of the Shih-Zhou-Lumley NLEVM¹⁰, where the C_μ value is no longer constant (like in the Realizable k- ϵ model) but it is expressed as a function of the shear invariant due to realizability constraints:

$$C_\mu = \frac{2/3}{3.9 + S} \quad (32)$$

This time S is the strain invariant, e.g.:

$$S = \frac{k}{\epsilon} \sqrt{\frac{1}{2} S_{ij} S_{ij}} \quad (33)$$

Moreover, the Reynolds stress tensor is expressed as follows:

$$\begin{aligned} \rho \overline{u_i' u_j'} = & \frac{2}{3} \rho k \delta_{ij} - \mu_t S_{ij} + C_1 \mu_t \frac{k}{\varepsilon} \left[S_{ik} S_{kj} - \frac{1}{3} \delta_{ij} S_{kl} S_{kl} \right] \\ & + C_2 \mu_t \frac{k}{\varepsilon} \left[\Omega_{ik} S_{kj} + \Omega_{jk} S_{ki} \right] \\ & + C_3 \mu_t \frac{k}{\varepsilon} \left[\Omega_{ik} \Omega_{jk} - \frac{1}{3} \delta_{ij} \Omega_{kl} \Omega_{kl} \right] \end{aligned} \quad (34)$$

The formulation of the coefficient C_1 , C_2 and C_3 is:

$$C_1 = \frac{C_{NL1}}{(C_{NL4} + C_{NL5} S^3) C_\mu} \quad (35)$$

$$C_2 = \frac{C_{NL2}}{(C_{NL4} + C_{NL5} S^3) C_\mu} \quad (36)$$

$$C_3 = \frac{C_{NL3}}{(C_{NL4} + C_{NL5} S^3) C_\mu} \quad (37)$$

The values of the constants CNL1, CNL3, CNL3, CNL4 and CNL5 are shown in Table V:

TABLE V
NLEVM coefficients

Constant	Value
C_{NL1}	0.8
C_{NL2}	11.0
C_{NL3}	4.5
C_{NL4}	1000.0
C_{NL5}	1.0

The non-linear eddy viscosity formulation is then coupled with the standard k - ε model of Launder and Spalding⁷. Note that the anisotropies and the realizability conditions for the present model are included in the new Reynolds stress tensor definition. The near-wall treatment is the same as the Realizable k - ε model, i.e. the Two-Layer formulation previously described.

III.B. Boundary condition and meshing convergence evaluation

Three different meshing configurations have been preliminarily studied in order to evaluate the influence of mesh size on the solution. The three unstructured mesh configurations (hereafter named as A, B, C) differ by a factor of around 2 on the mesh size in the first layer thickness and in the global size of a single mesh cell:

TABLE VI

Mesh Description

Configuration	First Layer Thickness	Major Size of a single Element	Number of Nodes
A	1×10^{-4} m	5×10^{-3} m	2,274,099
B	5×10^{-5} m	4×10^{-3} m	4,179,540
C	3×10^{-5} m	3×10^{-3} m	9,349,932

Values of the average wall y^+ are about 2.8, 1.4 and 0.8 respectively for configuration A, B and C. Meshing has been done using the ANSYS® Mesh module: an example of the inlet section mesh for the C configuration is shown in Figure 8:

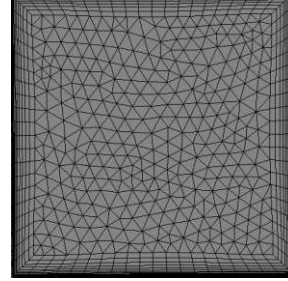


Figure 8 – Inlet section mesh for C configuration

A 13 m/s velocity inlet (Dirichlet) and a gauge pressure equal to 0 Pa pressure outlet (Neumann) boundary conditions are used. The working fluid is air at atmospheric temperature and pressure. The solver is the Pressure-based one and the Coupled pressure-velocity algorithm with pseudo-transient option is used. Gradients are evaluated through the Green-Gauss node-based method. Finally the Second Order Upwind Scheme is used for the spatial discretization of momentum, turbulent kinetic energy, turbulent dissipation rate (for the Realizable k - ε and the NLEVM models) or the specific dissipation rate (for the SST model).

Meshing convergence has been evaluated by comparing the average wall shear stress on the walls of the channel.

Table VII shows the results of the convergence evaluation for the three models:

TABLE VII

Average wall shear stress convergence evaluation

Configuration	Realizable k - ε	SST	NLEVM
A	0.940 Pa	1.001 Pa	0.948 Pa
B	0.916 Pa	0.984 Pa	0.923 Pa
C	0.917 Pa	0.988 Pa	0.910 Pa

From values in Table VI see that configuration C shows a converged wall shear stress solution both for Realizable k - ε and SST model and a difference of about 1.5% in the average wall shear stress for the NLEVM model. Based on these trends, we retained configuration C as the reference meshing, a finer grid leading to numerically unstable calculations, especially for the NLEVM.

III.C. Comparison with experimental data

A first model validation is done on the channel pressure drop (Table VIII):

TABLE VIII
Pressure Drop model validation

LDV or Model	Value [Pa]
LDV	488 ± 20
k- ϵ Real.	557.4
SST	549.3
NLEVM	512.4

The NLEVM model seems to provide a good pressure drop evaluation. Nevertheless it is worth analyzing the collected LDV data in order to better understand the most appropriate model to simulate the flow inside the channel.

With regard to the geometrical details given in Figure 6 and Figure 7 we are going to show the measurements of the X-velocity (hereafter “U”), Z-velocity (hereafter “W”) and XZ-Reynolds stress (hereafter “uw”). Figure 9 to Figure 17 show the comparison between experimental LDV data and numerical calculations with the three models previously described. Note that abscissas are non-dimensional coordinates (Y^* and Z^*) for the region of interest. In particular for the mixing zone the middle-plane (i.e. the plane where mixing occurs) is in $Y^*=0.5$.

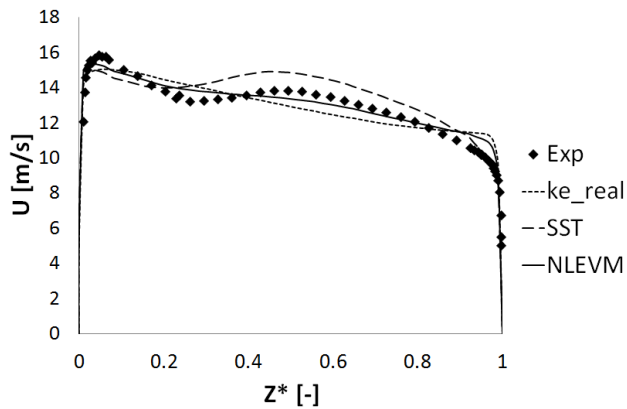


Figure 9 – U velocity comparison in line #1

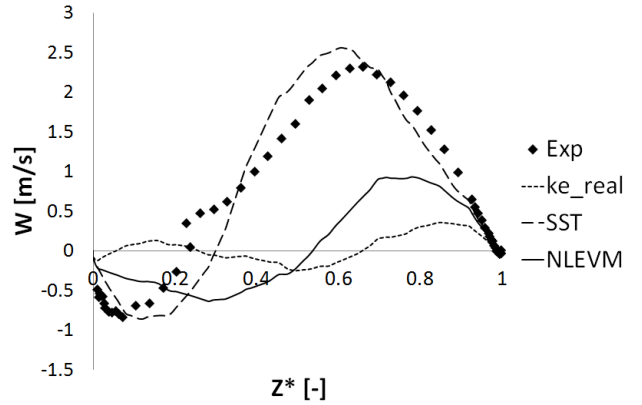


Figure 10 – W velocity comparison in line #1

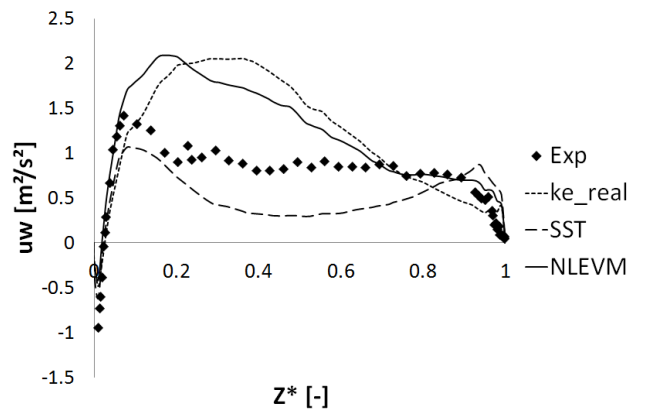


Figure 11 – uw Reynolds Stress comparison in line #1

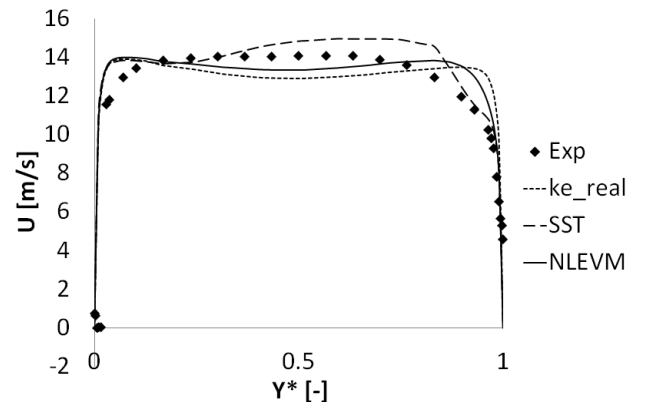


Figure 12 – U velocity comparison in line #2

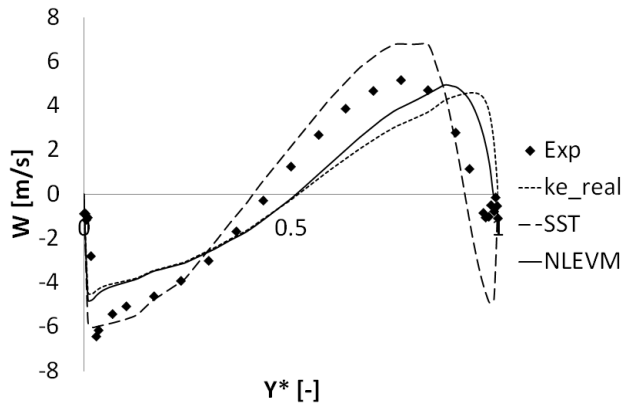


Figure 13 – W velocity comparison in line #2

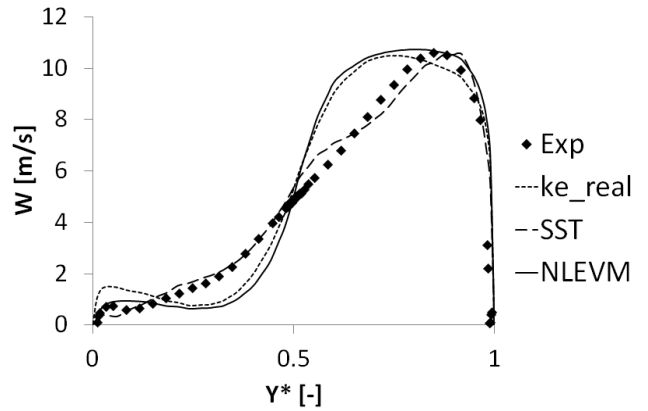


Figure 16 – W velocity comparison in line #3

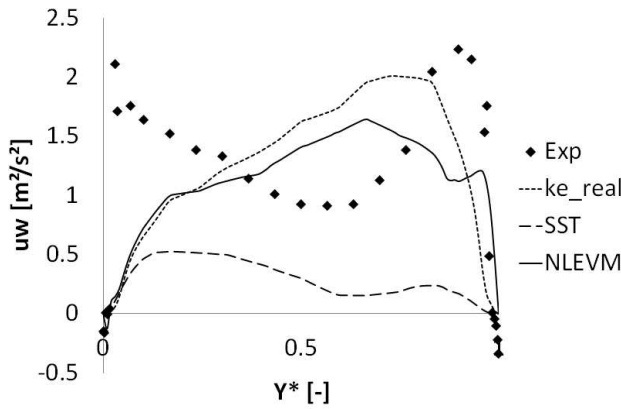


Figure 14 – uw Reynolds Stress comparison in line #1

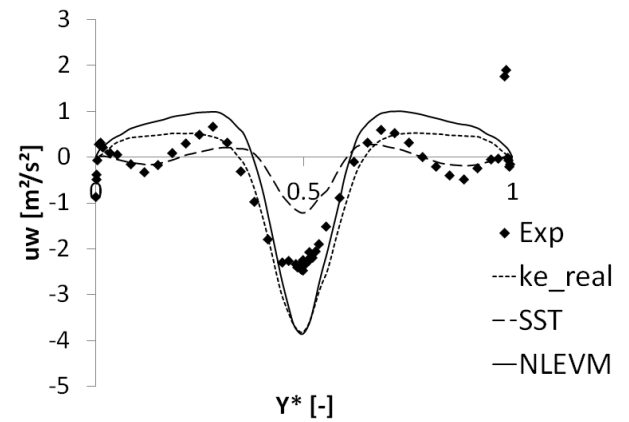


Figure 17 – uw Reynolds Stress comparison in line #1

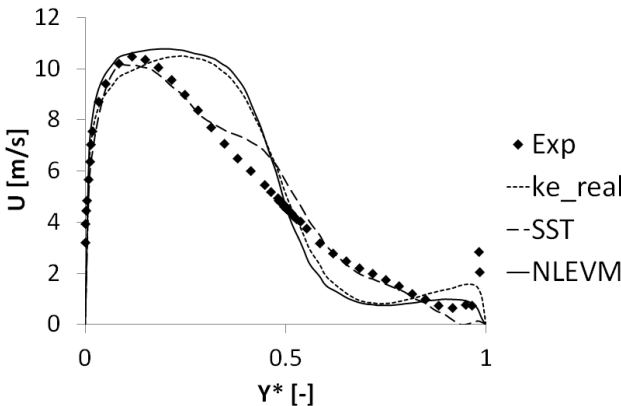


Figure 15 – U velocity comparison in line #3

As a general consideration, see that the SST model give the best overall results compared to the other models. As regards the in-bend flow, the SST model seems to provide very good results. Principal U velocity as well as radial W velocity profiles are very well calculated. On the other hand the uw Reynolds stress is generally under-predicted, still having a good global trend. The Realizable k- ϵ and the NLEVM model cannot reproduce the actual flow as precisely as the SST model.

The principal reasons are to be found in the fact that the ϵ -based formulation of the Realizable k- ϵ and the NLEV models is known not to work properly for adverse pressure gradient flows¹¹. Moreover the SST eddy viscosity formulation is known to give very good results for adverse pressure gradient boundary layers: in fact, even though the NLEVM model: in fact, even though the NLEVM model has an improved eddy viscosity formulation (i.e. through the variable C_μ), it is supposed to assure global model realizability rather than improve adverse pressure gradient boundary layers. For an in-bend flow this seems to be a critical deficiency. See Figure 18 to analyse the eddy viscosity distribution in the outer bend boundary layer in line 1:

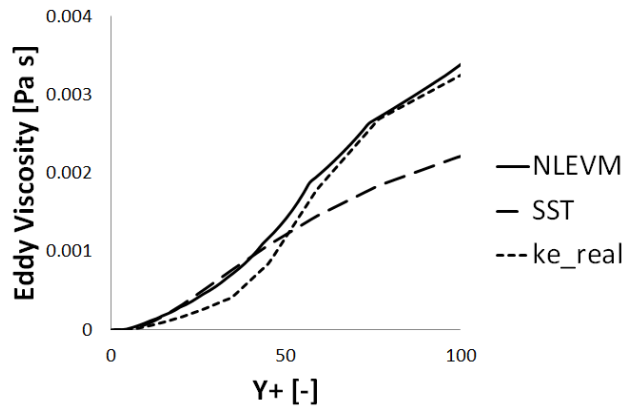


Figure 18 – Outer bnd boundary layer Eddy viscosity comparison in line#1

While the eddy viscosity in the viscous sublayer is quite the same for the three models (being a small fraction of the molecular viscosity in this region), differences appear in the outer boundary layer. There is a factor of about two between the eddy viscosity calculated by the Realizable $k-\epsilon$ and the NLEV models and the one calculated by the SST. See indeed the high velocity gradient eddy viscosity limiter in the SST formulation, which seems to act very well in the near wall region; this is not necessarily true for the Realizable $k-\epsilon$ and the NLEV models. Hence it appears that the formulation of the eddy viscosity used in a very similar way in the Realizable $k-\epsilon$ and the NLEV model (Eq. 6 and Eq.32) gives very similar results but does not work properly, at least for adverse pressure gradient flows.

As regards the mixing zone, first of all note that there are two isolated points in the boundary layer at $Y^* \approx 1$ both in Figure 15 and Figure 17: they are likely spurious experimental points where the LDV system measured a false value either due to proximity to the glass window or to a DEHS spot deposited in the glass window. Anyway the SST model correctly represents the two velocity components U and W and gives a good trend for the uw Reynolds stress. Concerning the Realizable $k-\epsilon$ and the NLEVM model, the velocity profiles are not in good agreement with the experimental data and the uw stress, although it is good regarding the global range of values, does not have the right trend in the near middle-plane ($Y^* = 0.5$) region as well as in the near-wall region. A possible explanation for this behaviour likely lays again in the turbulence kinetic energy production term (Eq.29): this production limiter is supposed to make the model quasi-realizable, setting a necessary upper bound on the turbulence kinetic energy production term as shown by Durbin¹².

See in Figure 19 the turbulence kinetic energy production profiles in the three models:

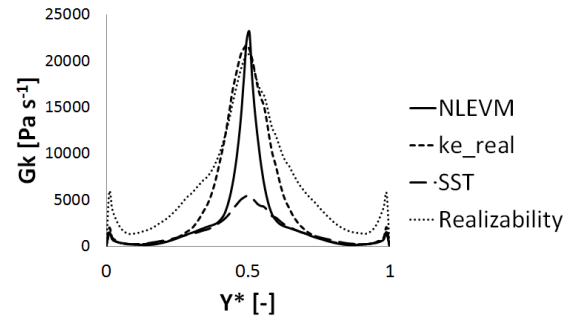


Figure 19 – Turbulence Kinetic Energy Production term comparison in line#3

Together with the turbulence kinetic energy production term for the three used models, a Realizability plot is also shown, based on the upper bound proposed by Durbin¹² and Park and Park¹³. An actual improvement in the modelling of this term seems to be the limiter in the SST model. This limiter is supposed to improve the model behaviour in stagnation points¹⁴: indeed the mixing zone middle plane seems to represent a zone of turbulence kinetic energy build-up due to the counter-converging two flows. Indeed all the three models respect the Realizability condition; nevertheless, the SST model is the only one that do not reach the Realizability-imposed limit in the middle of the mixing zone. Therefore the higher turbulence kinetic energy production both for the Realizable $k-\epsilon$ and the NLEV model in this zone provides an excessive turbulence kinetic energy, which gives a too much high value of the eddy viscosity along the Y direction: this results in a higher flow diffusion along the X and Z directions limiting the flow penetration along Y direction. This finally results in a more typical “all-alone” flow profile (e.g. not enough mixing), as those of Figure 15 and Figure 16.

IV. CONCLUSIONS

From this analysis it can be stated that the SST model gives very satisfactory results for the complex flow presented, even being a RANS two-equation model: it provides a good description of the fluid flow and a slight pressure drop overestimation. The Realizable $k-\epsilon$ almost never gives the good trends, still suffering the well-known deficiencies of all $k-\epsilon$ based models. The NLEVM formulation coupled with the Standard $k-\epsilon$ model works slightly better than the Realizable $k-\epsilon$ model, giving a good prediction of the pressure drop but still presenting many deficiencies regarding the fluid flow description. In particular the major features providing such good results for the SST model seem to be the good in-bend flow description given by an ω -based model (like the SST), the turbulence kinetic energy production limiter and the eddy viscosity formulation: they actually prevent the turbulence kinetic energy build-up that provides an erroneous prevision of both in-bend and mixing zone when

Realizable k-ε and the NLEV models are used. Moreover, despite the fact that a non-isotropic model would be supposed to give better results for such a complex flow, this seems not to be the case if the non-isotropic model cannot correctly represent the global flow inside the different parts of the channel (in this case the k-ε model cannot correctly represent the in-bend flow).

Indeed the results given by the SST model are valuable considering the complexity of this wall-bounded flow. Hence its utilisation is strongly recommended for the description and the following numerical studies in the present geometrical configuration.

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NOMENCLATURE

CFD: Computational Fluid Dynamics
 ASTRID: Advanced Sodium Technological Reactor for Industrial Demonstration
 GENIV: Generation IV International Forum
 SFR: Sodium-cooled Fast Reactor
 PCHE: Printed Circuit Heat Exchanger
 PSHE: Plate Stamped Heat Exchanger
 2-C: 2 component (i.e. of velocity vector)
 LDV: Laser Doppler Velocimetry
 σ: Standard deviation for a statistical distribution
 U_i: i-mean velocity component
 u_i: i-fluctuating velocity component
 ρ: Fluid density
 k: Turbulence kinetic energy (TKE)
 μ: Molecular dynamic viscosity
 μ_t: Eddy viscosity
 ε: Turbulence dissipation rate (TDR)
 σ_k: TKE Prandtl number
 σ_ε: TDR Prandtl number
 ω: Specific dissipation rate (SDR)
 σ_ω: SDR Prandtl number
 y: distance to the nearest wall
 $S_{ij} = \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i}$ Deformation rate
 $\Omega_{ij} = \frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i}$ Rotation rate
 Y+: non-dimensional distance from the wall

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